AIEEE-CBSE-ENG-03

1. A function f from the set of natural numbers to integers defined by

$$f(n) = \begin{cases} \frac{n-1}{2}, & \text{when is odd} \\ -\frac{n}{2}, & \text{when n is even} \end{cases}$$

- (A) one-one but not onto
- (B) onto but not one-one
- (C) one-one and onto both
- (D) neither one-one nor onto
- 2. Let z_1 and z_2 be two roots of the equation $z^2 + az + b = 0$, z being complex. Further, assume that the origin, z_1 and z_2 form an equilateral triangle, then
 - (A) $a^2 = b$

(B) $a^2 = 2b$

(C) $a^2 = 3b$

- (D) $a^2 = 4b$
- 3. If z and ω are two non–zero complex numbers such that $|z\omega|=1$, and Arg (z) –

Arg
$$(\omega) = \frac{\pi}{2}$$
, then $\overline{z}\omega$ is equal to

(A) 1

(B) - 1

(C) i

(D) -

4. If
$$\left(\frac{1+i}{1-i}\right)^x = 1$$
, then

- (A) x = 4n, where n is any positive integer
- (B) x = 2n, where n is any positive integer
- (C) x = 4n + 1, where n is any positive integer
- (D) x = 2n + 1, where n is any positive integer
- 5. If $\begin{vmatrix} a & a^2 & 1+a^3 \\ b & b^2 & 1+b^3 \\ c & c^2 & 1+c^3 \end{vmatrix} = 0$ and vectors (1, a, a^2) (1, b, b^2) and (1, c, c^2) are non-

coplanar, then the product abc equals

(A) 2

(B) - 1

(C) 1

- (D) 0
- 6. If the system of linear equations

$$x + 2ay + az = 0$$

$$x + 3by + bz = 0$$

$$x + 4cy + cz = 0$$

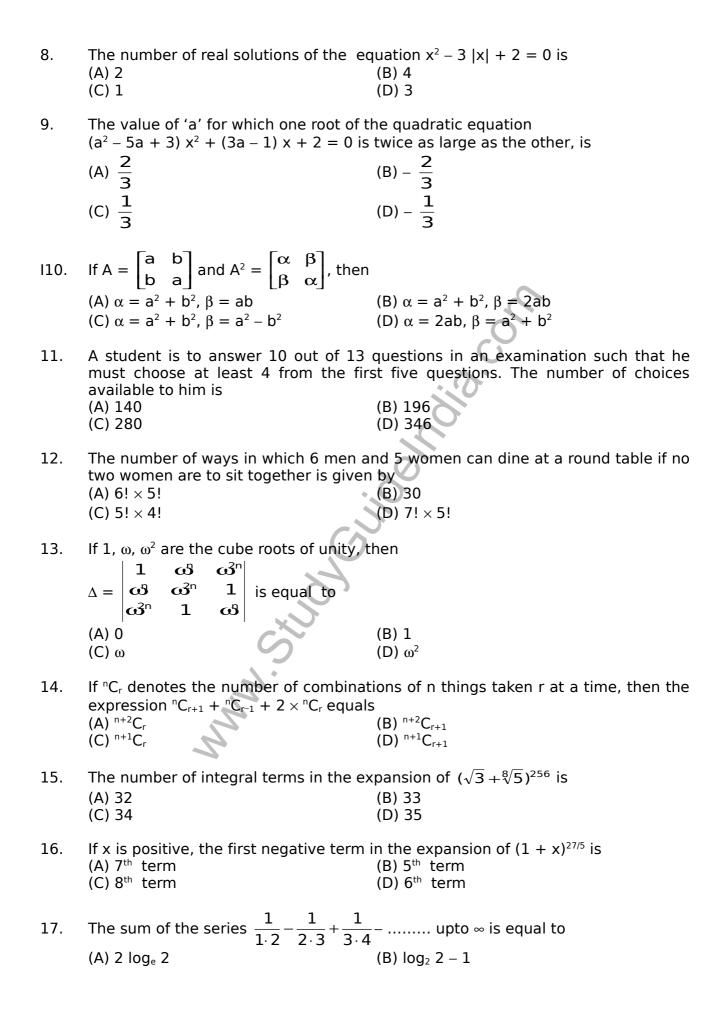
has a non-zero solution, then a, b, c

(A) are in A. P.

(B) are in G.P.

(C) are in H.P.

- (D) satisfy a + 2b + 3c = 0
- 7. If the sum of the roots of the quadratic equation $ax^2 + bx + c = 0$ is equal to the sum of the squares of their reciprocals, then $\frac{a}{c}$, $\frac{b}{a}$ and $\frac{c}{b}$ are in
 - (A) arithmetic progression
- (B) geometric progression
- (C) harmonic progression
- (D) arithmetic-geometric-progression



20.	The sum of the radii of inscribed and circumscribed circles for an n sided regular polygon of side a, is		
	(A) a cot $\left(\frac{\pi}{n}\right)$	(B) $\frac{a}{2} \cot \left(\frac{\pi}{2n} \right)$	
	(C) a $\cot\left(\frac{\pi}{2n}\right)$	(D) $\frac{a}{4} \cot \left(\frac{\pi}{2n} \right)$	
21.	If in a triangle ABC a $\cos^2\left(\frac{C}{2}\right)$ + c $\cos^2\left(\frac{C}{2}\right)$	$s^2\left(\frac{A}{2}\right) = \frac{3b}{2}$, then the sides a, b and c	
	(A) are in A.P. (C) are in H.P.	(B) are in G.P.(D) satisfy a + b = c	
22.	In a triangle ABC, medians AD and BE	are drawn. If AD = 4, \angle DAB = $\frac{\pi}{6}$ and \angle	
	ABE = $\frac{\pi}{3}$, then the area of the \triangle ABC is		
	(A) $\frac{8}{3}$	(B) $\frac{16}{3}$	
	(A) $\frac{8}{3}$ (C) $\frac{32}{3}$	(B) $\frac{16}{3}$ (D) $\frac{64}{3}$	
23.	The trigonometric equation $\sin^{-1} x = 2 \sin^{-1} a$, has a solution for		
	(A) $\frac{1}{2} < a < \frac{1}{\sqrt{2}}$	(B) all real values of a	
	(C) $ a < \frac{1}{2}$	(D) $ a \ge \frac{1}{\sqrt{2}}$	
24.	24. The upper $\frac{3}{4}$ th portion of a vertical pole subtends an angle $\tan^{-1} \frac{3}{5}$ at		
	•	and at a distance 40 m from the foot. A	
		(B) 40 m (D) 80 m	
25.		s inverse gives the minimum value of the	
	sum at x equal to (A) 2 (C) – 1	(B) 1 (D) – 2	

(D) $\log_{e}\left(\frac{4}{e}\right)$

(B) lie on an ellipse

(D) are vertices of a triangle

(D) arithmetic–geometric progression

Let f(x) be a polynomial function of second degree. If f(1) = f(-1) and a, b, c

If x_1 , x_2 , x_3 and y_1 , y_2 , y_3 are both in G.P. with the same common ratio, then the

(B) G.P.

(C) log_e 2

(A) A.P.

(C) H. P.

are in A. P., then f' (a), f' (b) and f' (c) are in

points (x_1, y_1) (x_2, y_2) and (x_3, y_3)

(A) lie on a straight line

(C) lie on a circle

18.

19.

26. If
$$f: R \to R$$
 satisfies $f(x + y) = f(x) + f(y)$, for all $x, y \in R$ and $f(1) = 7$, then
$$\sum_{r=1}^{n} f(r)$$
 is

(A)
$$\frac{7n}{2}$$

(B)
$$\frac{7(n+1)}{2}$$

(B)
$$\frac{7(n+1)}{2}$$

(D) $\frac{7n(n+1)}{2}$

27. If f (x) = xⁿ, then the value of f (1)
$$-\frac{f'(1)}{1!} + \frac{f''(1)}{2!} - \frac{f'''(1)}{3!} + \dots + \frac{(-1)^n f^n(1)}{n!}$$
 is (A) 2ⁿ (B) 2ⁿ⁻¹ (D) 1

(D)
$$1$$

28. Domain of definition of the function
$$f(x) = \frac{3}{4-x^2} + \log_{10}(x^3 - x)$$
, is

(B)
$$(-1, 0) \cup (1, 2)$$

(C)
$$(1, 2) \cup (2, \infty)$$

(D)
$$(-1, 0) \cup (1, 2) \cup (2, \infty)$$

29.
$$\lim_{x \to \pi/2} \frac{\left[1 - \tan\left(\frac{x}{2}\right)\right] [1 - \sin x]}{\left[1 + \tan\left(\frac{x}{2}\right)\right] [\pi - 2x]^3}$$
 is

(A)
$$\frac{1}{8}$$

(C)
$$\frac{1}{32}$$

30. If
$$\lim_{x\to 0} \frac{\log(3+x)-\log(3-x)}{x} = k$$
, the value of k is

(B)
$$-\frac{1}{3}$$

(C)
$$\frac{2}{3}$$

(D)
$$-\frac{2}{3}$$

31. Let
$$f(a) = g(a) = k$$
 and their n^{th} derivatives $f^n(a)$, $g^n(a)$ exist and are not equal for some n. Further if $\lim_{x\to a} \frac{f(a)g(x)-f(a)-g(a)f(x)+g(a)}{g(x)-f(x)} = 4$, then the value

of k is

(A) 4

(B) 2

(C) 1

(D) 0

32. The function
$$f(x) = \log(x + \sqrt{x^2 + 1})$$
, is

(A) an even function

(B) an odd function

(C) a periodic function

(D) neither an even nor an odd function

33. If
$$f(x) = \begin{cases} xe^{-\left(\frac{1}{|x|}, \frac{1}{x}\right)}, & x \neq 0 \text{ then } f(x) \text{ is } \\ 0, & x = 0 \end{cases}$$

- (A) continuous as well as differentiable for all x
- (B) continuous for all x but not differentiable at x = 0
- (C) neither differentiable nor continuous at x = 0
- (D) discontinuous everywhere
- If the function $f(x) = 2x^3 9ax^2 + 12a^2 x + 1$, where a > 0, attains its maximum 34. and minimum at p and q respectively such that $p^2 = q$, then a equals
 - (A) 3

(C) 2

35. If
$$f(y) = e^y$$
, $g(y) = y$; $y > 0$ and $F(t) = \int_0^t f(t - y) g(y) dy$, then

- (A) F (t) = $1 e^{-t} (1 + t)$

(C) $F(t) = t e^{t}$

36. If
$$f(a + b - x) = f(x)$$
, then $\int_{a}^{b} \times f(x) dx$ is equal to

- (A) $\frac{a+b}{2}\int_{a}^{b}f(b-x)dx$

- (C) $\frac{b-a}{2}\int_{0}^{b}f(x)dx$
- (B) $\frac{a+b}{2} \int_{a}^{b} f(x) dx$ (D) $\frac{a+b}{2} \int_{a}^{b} f(a+b-x) dx$

37. The value of
$$\lim_{x\to 0} \frac{\int_{0}^{x^2} \sec^2 t \, dt}{x \sin x}$$
 is

(A) 3

(C) 1

38. The value of the integral
$$I = \int_{0}^{1} x (1-x)^{n} dx$$
 is

(A) $\frac{1}{n+1}$

(C) $\frac{1}{n+1} - \frac{1}{n+2}$

(D) $\frac{1}{n+1} + \frac{1}{n+2}$

$$39. \quad \lim_{n\to\infty}\frac{1+2^4+3^4+\ldots\ldots+n^4}{n^5}-\lim_{n\to\infty}\frac{1+2^3+3^3+\ldots\ldots+n^3}{n^5} \ is$$

(A) $\frac{1}{30}$

(B) zero



(D)
$$\frac{1}{5}$$

Let $\frac{d}{dx}F(x) = \left(\frac{e^{\sin x}}{x}\right)$, x > 0. If $\int_{1}^{4} \frac{3}{x}e^{\sin x^3} dx = F(k) - F(1)$, then one of the 40.

possible values of k, is

(B) 16

(D) 64

The area of the region bounded by the curves y = |x - 1| and y = 3 - |x| is 41.

(A) 2 sa units

(B) 3 sq units

(C) 4 sq units

(D) 6 sq units

Let f (x) be a function satisfying f' (x) = f (x) with f (0) = 1 and g (x) be a function 42. that satisfies $f(x) + g(x) = x^2$. Then the value of the integral $\int_0^x f(x) g(x) dx$, is

(A)
$$e - \frac{e^2}{2} - \frac{5}{2}$$

(B)
$$e + \frac{e^2}{2} - \frac{3}{2}$$

(C)
$$e - \frac{e^2}{2} - \frac{3}{2}$$

(D)
$$e + \frac{e^2}{2} + \frac{5}{2}$$

43. The degree and order of the differential equation of the family of all parabolas whose axis is x-axis, are respectively

The solution of the differential equation $(1 + y^2) + (x - e^{\tan^{-1} y}) \frac{dy}{dx} = 0$, is 44.

(A)
$$(x-2) = k e^{-\tan^{-1} y}$$

(C) $x e^{\tan^{-1} y} = \tan^{-1} y + k$

(B)
$$2x e^{2 \tan^{-1} y} + k$$

(C)
$$x e^{\tan^{-1} y} = \tan^{-1} y + k$$

(D)
$$x e^{2 \tan^{-1} y} = e^{\tan^{-1} y} + k$$

If the equation of the locus of a point equidistant from the points (a_1, b_1) and (a_2, b_2) 45. b_2) is $(a_1 - a_2) x + (b_1 - b_2) y + c = 0$, then the value of 'c' is

(A)
$$\frac{1}{2}(a_2^2+b_2^2-a_1^2-b_1^2)$$

(B)
$$a_1^2 + a_2^2 + b_1^2 - b_2^2$$

(C)
$$\frac{1}{2}(a_1^2 + a_2^2 - b_1^2 - b_2^2)$$

(D)
$$\sqrt{a_1^2 + b_1^2 - a_2^2 - b_2^2}$$

46. Locus of centroid of the triangle whose vertices are (a cos t, a sin t), (b sin t, - b cos t) and (1, 0), where t is a parameter, is

(A)
$$(3x-1)^2 + (3y)^2 = a^2 - b^2$$

(B)
$$(3x - 1)^2 + (3y)^2 = a^2 + b^2$$

(C)
$$(3x + 1)^2 + (3y)^2 = a^2 + b^2$$
 (D) $(3x + 1)^2 + (3y)^2 = a^2 - b^2$

(D)
$$(3x + 1)^2 + (3y)^2 = a^2 - b^2$$

If the pair of straight lines $x^2 - 2pxy - y^2 = 0$ and $x^2 - 2qxy - y^2 = 0$ be such that 47. each pair bisects the angle between the other pair, then

$$(A) p = q$$

(B)
$$p = -q$$

(C)
$$pq = 1$$

(D)
$$pq = -1$$

- 48. a square of side a lies above the x-axis and has one vertex at the origin. The side passing through the origin makes an angle α (0 < α < $\frac{\pi}{4}$) with the positive direction of x-axis. The equation of its diagonal not passing through the origin is
 - (A) $y (\cos \alpha \sin \alpha) x (\sin \alpha \cos \alpha) = a$
 - (B) $y (\cos \alpha + \sin \alpha) + x (\sin \alpha \cos \alpha) = a$
 - (C) $y(\cos \alpha + \sin \alpha) + x(\sin \alpha + \cos \alpha) = a$
 - (D) $y (\cos \alpha + \sin \alpha) + x (\cos \alpha \sin \alpha) = a$
- If the two circles $(x 1)^2 + (y 3)^2 = r^2$ and $x^2 + y^2 8x + 2y + 8 = 0$ intersect in 49. two distinct points, then
 - (A) 2 < r < 8

(B) r < 2

(C) r = 2

- (D) r > 2
- The lines 2x 3y = 5 and 3x 4y = 7 are diameters of a circle having area as 50. 154 sq units. Then the equation of the circle is
 - (A) $x^2 + y^2 + 2x 2y = 62$
- (C) $x^2 + y^2 2x + 2y = 47$
- (B) $x^2 + y^2 + 2x 2y = 47$ (D) $x^2 + y^2 2x + 2y = 62$
- The normal at the point $(bt_1^2, 2bt_1)$ on a parabola meets the parabola again in the 51. point (bt₂², 2bt₂), then
 - (A) $t_2 = -t_1 \frac{2}{t_1}$

(D) $t_2 = t_1 - \frac{2}{t_1}$

- The foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{b^2} = 1$ and the hyperbola $\frac{x^2}{144} \frac{y^2}{81} = \frac{1}{25}$ coincide. 52.
 - Then the value of b2 is
 - (A) 1

(C)7

- A tetrahedron has vertices at O (0, 0, 0), A (1, 2, 1), B (2, 1, 3) and C (-1, 1, 2). 53. Then the angle between the faces OAB and ABC will be

(B) $\cos^{-1}\left(\frac{17}{31}\right)$

- The radius of the circle in which the sphere $x^2 + y^2 + z^2 + 2x 2y 4z 19 = 0$ is 54. cut by the plane x + 2y + 2z + 7 = 0 is
 - (A) 1

(B) 2

(C) 3

- The lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$ and $\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$ are coplanar if 55.
 - (A) k = 0 or -1

(C) k = 0 or -3

- (D) k = 3 or -3
- 56. The two lines x = ay + b, z = cy + d and x = a'y + b', z = c'y + d' will be perpendicular, if and only if
 - (A) aa' + bb' + cc' + 1 = 0
- (B) aa' + bb' + cc' = 0

(C)
$$(a + a') (b + b') + (c + c') = 0$$

(D)
$$aa' + cc' + 1 = 0$$

57. The shortest distance from the plane 12x + 4y + 3z = 327 to the sphere $x^2 + y^2 + z^2 + 4x - 2y - 6z = 155$ is

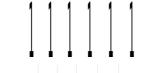
(A) 26

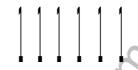
(B) $11\frac{4}{13}$

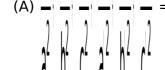
(C) 13

(D) 39

58. Two systems of rectangular axes have the same origin. If a plane cuts them at distances a, b, c and a', b', c' from the origin, then



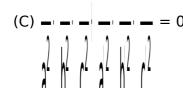


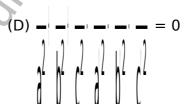












59. a, b, c are 3 vectors, such that a+b+c=0, |a|=1, |b|=2, |c|=3, then $a\cdot b+b\cdot c+c\cdot a$ is equal to

(A) 0

(B) - 7

(C) 7

(D) 1

60. If u, v and w are three non-coplanar vectors, then $(u+v-w)\cdot(u-v)\times(v-w)$ equals

(A) 0

(B) $u \cdot v \times w$

(C) $u \cdot w \times v$

(D) $3u \cdot v \times w$

61. Consider points A, B, C and D with position vectors $7\hat{i} - 4\hat{j} + 7\hat{k}$, $\hat{i} - 6\hat{j} + 10\hat{k}$, $-\hat{i} - 3\hat{j} + 4\hat{k}$ and $5\hat{i} - \hat{j} + 5\hat{k}$ respectively. Then ABCD is a

(A) square

(B) rhombus

(C) rectangle

(D) parallelogram but not a rhombus

62. The vectors $\overrightarrow{AB} = 3\hat{i} + 4\hat{k}$, and $\overrightarrow{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$ are the sides of a triangle ABC. The length of the median through A is

(A) √18

(B) $\sqrt{72}$

	(C) √33	(D) √288
63.	from the point $\hat{i} + 2\hat{j} + 3\hat{k}$ to the point forces is	tes $4\hat{i} + \hat{j} - 3\hat{k}$ and $3\hat{i} + \hat{j} - \hat{k}$ is displaced nt $5\hat{i} + 4\hat{j} + \hat{k}$. The total work done by the
	(A) 20 units (C) 40 units	(B) 30 units (D) 50 units
64.	Let $u = \hat{i} + \hat{j}$, $v = \hat{i} - \hat{j}$ and $w = \hat{i} + 2\hat{j} + 2j$	-3 \hat{k} . If \hat{n} is unit vector such that $u \cdot \hat{n} = 0$ (B) 1 (D) 3
65.	observations of the set is increased by (A) is increased by 2	servations is 20.5. If each of the largest 4 y 2, then the median of the new set (B) is decreased by 2 (D) remains the same as that of the
66.	available: $\sum x^2 = 2830$, $\sum x = 170$	und to be wrong and was replaced by the variance is (B) 188.66 (D) 8.33
67.	Five horses are in a race. Mr. A select them. The probability that Mr. A select (A) $\frac{4}{5}$ (C) $\frac{1}{5}$	is two of the horses at random and bets on ted the winning horse is (B) $\frac{3}{5}$ (D) $\frac{2}{5}$
68.	Events A, B, C are mutually exclusive events such that P (A) = $\frac{3x+1}{3}$, P (B) =	
	$\frac{1-x}{4} \text{ and}$ values of x are in the interval $(A) \left[\frac{1}{3}, \frac{1}{2}\right]$ $(C) \left[\frac{1}{3}, \frac{13}{3}\right]$	P (C) = $\frac{1-2x}{2}$. The set of possible (B) $\left[\frac{1}{3}, \frac{2}{3}\right]$ (D) [0, 1]
69.	The mean and variance of a random variance of a ra	variable having a binomial distribution are 4 $ \text{(B) } \frac{1}{16} \\ \text{(D) } \frac{1}{4} $

70.	•	\boldsymbol{R} . If \boldsymbol{Q} is doubled then \boldsymbol{R} is doubled. If	
	the direction of \mathbf{Q} is reversed, then \mathbf{R} is again doubled. Then $\mathbf{P}^2:\mathbf{Q}^2:\mathbf{R}^2$ is		
	(A) 3:1:1	(B) 2:3:2	
	(C) 1 : 2 : 3	(D) 2:3:1	
71.	Let R_1 and R_2 respectively be the maximum ranges up and down an incline plane and R be the maximum range on the horizontal plane. Then R_1 , R , R_2 are in		
	(A) arithmetic–geometric progression		
	(C) G.P.	(D) H.P.	

- 72. A couple is of moment G and the force forming the couple is P. If P is turned through a right angle, the moment of the couple thus formed is H. If instead, the forces P are turned through an angle α , then the moment of couple becomes
 - (A) $G \sin \alpha H \cos \alpha$ (B) $H \cos \alpha + G \sin \alpha$ (C) $G \cos \alpha H \sin \alpha$ (D) $H \sin \alpha G \cos \alpha$
- 73. Two particles start simultaneously from the same point and move along two straight lines, one with uniform velocity ${\bf u}$ and the other from rest with uniform acceleration ${\bf f}$. Let α be the angle between their directions of motion. The relative velocity of the second particle with respect to the first is least after a time
 - (A) $\frac{u\sin\alpha}{f}$ (B) $\frac{f\cos\alpha}{u}$ (C) $u\sin\alpha$ (D) $\frac{u\cos\alpha}{f}$
- 74. Two stones are projected from the top of a cliff h meters high, with the same speed u so as to hit the ground at the same spot. If one of the stones is projected horizontally and the other is projected at an angle θ to the horizontal then tan θ equals

 (A) 2u
 - (A) $\sqrt{\frac{2u}{gh}}$ (B) $2g\sqrt{\frac{u}{h}}$ (C) $2h\sqrt{\frac{u}{g}}$ (D) $u\sqrt{\frac{2}{gh}}$
- 75. A body travels a distances s in t seconds. It starts from rest and ends at rest. In the first part of the journey, it moves with constant acceleration f and in the second part with constant retardation r. The value of t is given by
 - (A) $2s\left(\frac{1}{f} + \frac{1}{r}\right)$ (B) $\frac{1}{f} + \frac{1}{r}$ (C) $\sqrt{2s(f+r)}$ (D) $\sqrt{2s\left(\frac{1}{f} + \frac{1}{r}\right)}$

Solutions

1. Clearly both one – one and onto Because if n is odd, values are set of all non-negative integers and if n is an even, values are set of all negative integers.

Hence, (C) is the correct answer.

2. $z_1^2 + z_2^2 - z_1 z_2 = 0$ $(z_1 + z_2)^2 - 3z_1z_2 = 0$ $a^2 = 3b$.

Hence, (C) is the correct answer.

 $\begin{vmatrix} a & a^{2} & 1 \\ b & b^{2} & 1 \\ c & c^{2} & 1 \end{vmatrix} + \begin{vmatrix} 1 & a & a^{2} \\ 1 & b & b^{2} \\ 1 & c & c^{2} \end{vmatrix} = 0$ $(1 + abc) \begin{vmatrix} a & a^{2} & 1 \\ b & b^{2} & 1 \\ c & c^{2} & 1 \end{vmatrix} = 0$ 5.

$$(1 + abc) \begin{vmatrix} a & a^2 & 1 \\ b & b^2 & 1 = 0 \\ c & c^2 & 1 \end{vmatrix}$$

$$\Rightarrow$$
 abc = -1 .

Hence, (B) is the correct answer

 $\frac{1+i}{1-i} = \frac{(1+i)^2}{2} = i$ 4. $\left(\frac{1+i}{1-i}\right)^{x} = i^{x}$

$$\left(\frac{1-i}{1-i}\right) = i$$

$$\Rightarrow x = 4n$$

Hence, (A) is the correct answer.

Coefficient determinant = $|\mathbf{1}|$ 6.

$$\Rightarrow b = \frac{2ac}{a+c}.$$

Hence, (C) is the correct answer

 $x^{2} - 3 |x| + 2 = 0$ (|x| - 1) (|x| - 2) = 0 8.

 \Rightarrow x = \pm 1, \pm 2. Hence, (B) is the correct answer

7. Let α , β be the roots

$$\alpha + \beta = \frac{1}{\alpha^2} + \frac{1}{\beta^2}$$

$$\alpha + \beta = \frac{\alpha^2 + \beta^2 - 2\alpha\beta}{(\alpha + \beta)}$$

$$\left(-\frac{b}{a}\right) = \frac{b^2 - 2ac}{c^2}$$

$$\Rightarrow$$
 2a²c = b (a² + bc)

$$\Rightarrow \frac{a}{c}, \frac{b}{a}, \frac{c}{b}$$
 are in H.P.

Hence, (C) is the correct answer

10.
$$A = \begin{bmatrix} a & b \\ b & a \end{bmatrix}$$

$$A^{2} = \begin{bmatrix} a & b \\ b & a \end{bmatrix} \begin{bmatrix} a & b \\ b & a \end{bmatrix}$$

$$= \begin{bmatrix} a^{2} + b^{2} & 2ab \\ 2ab & a^{2} + b^{2} \end{bmatrix}$$

$$\Rightarrow \alpha = a^{2} + b^{2}, \beta = 2ab.$$
Hence, (B) is the correct answer.

9.
$$\beta = 2\alpha$$

$$3\alpha = \frac{3a-1}{a^2-5a+3}$$

$$2\alpha^2 = \frac{2}{a^2-5a+6}$$

$$\frac{(3a-1)^2}{a(a^2-5a+3)^2} = \frac{1}{a^2+5a+6}$$

$$\Rightarrow a = \frac{2}{3}$$
Hence, (A) is the correct answer

nerice, (A) is the correct answer

- 12. Clearly $5! \times 6!$ (A) is the correct answer
- 11. Number of choices = ${}^5C_4 \times {}^8C_6 + {}^5C_5 \times {}^8C_5$ = 140 + 56. Hence, (B) is the correct answer

13.
$$\Delta = \begin{vmatrix} 1 + \omega^{1} + \omega^{2} & \omega^{1} & \omega^{3} \\ 1 + \omega^{1} + \omega^{2} & \omega^{2} & 1 \\ 1 + \omega^{1} + \omega^{2} & 1 & \omega^{2} \end{vmatrix}$$
$$= 0$$

Since, $1+\omega^n+\omega^{2n}=0$, if n is not a multiple of 3 Therefore, the roots are identical. Hence, (A) is the correct answer

14.
$${}^{n}C_{r+1} + {}^{n}C_{r-1} + {}^{n}C_{r} + {}^{n}C_{r}$$

= ${}^{n+1}C_{r+1} + {}^{n+1}C_{r}$
= ${}^{n+2}C_{r+1}$.
Hence, (B) is the correct answer

17.
$$\frac{1}{1 \cdot 2} - \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} - \dots$$

$$= 1 - \frac{1}{2} - \frac{1}{2} + \frac{1}{3} + \frac{1}{3} - \frac{1}{4} - \dots$$

$$= 1 - 2\left(\frac{1}{2} - \frac{1}{3} + \frac{1}{4} - \dots\right)$$

$$= 2\left(1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots\right) - 1$$
$$= 2 \log 2 - \log e$$
$$= \log\left(\frac{4}{e}\right).$$

Hence, (D) is the correct answer.

- 15. General term = $^{256}C_r$ ($\sqrt{3}$) $^{256-r}$ [(5) $^{1/8}$]^r From integral terms, or should be 8k \Rightarrow k = 0 to 32. Hence, (B) is the correct answer.
- 18. $f(x) = ax^2 + bx + c$ f(1) = a + b + c f(-1) = a - b + c $\Rightarrow a + b + c = a - b + c$ also 2b = a + c f'(x) = 2ax + b = 2ax $f'(a) = 2a^2$ f'(b) = 2ab f'(c) = 2ac $\Rightarrow AP$. Hence, (A) is the correct answer.
- 19. Result (A) is correct answer.
- 20. (B)
- 21. $a\left(\frac{1+\cos C}{2}\right)+c\left(\frac{1+\cos A}{2}\right)=\frac{3b}{2}$ $\Rightarrow a+c+b=3b$ a+c=2b.Hence, (A) is the correct answer
- 26. f(1) = 7 f(1 + 1) = f(1) + f(1) $f(2) = 2 \times 7$ only $f(3) = 3 \times 7$ $\sum_{r=1}^{n} f(r) = 7 (1 + 2 + \dots + n)$ $= 7 \frac{n(n+1)}{2}.$
- 25. (B)

23.
$$-\frac{\pi}{4} \le \frac{\sin^2 x}{2} \le \frac{\pi}{4}$$
$$-\frac{\pi}{4} \le \sin^{-1}(a) \le \frac{\pi}{4}$$
$$\frac{1}{2} \le |a| \le \frac{1}{\sqrt{2}}.$$

Hence, (D) is the correct answer

27. LHS =
$$1 - \frac{n}{1!} + \frac{n(n-1)}{2!} - \frac{n(n-1)(n-2)}{3!} + \dots$$

= $1 - {^{n}C_{1}} + {^{n}C_{2}} - \dots$
= 0.
Hence, (C) is the correct answer

30.
$$\lim_{x\to 0} \frac{\frac{1}{3+x} + \frac{1}{3-x}}{1} = \frac{2}{3}$$

Hence, (C) is the correct answer.

28.
$$4 - x^{2} \neq 0$$

$$\Rightarrow x \neq \pm 2$$

$$x^{3} - x > 0$$

$$\Rightarrow x (x + 1) (x - 1) > 0.$$
Hence (D) is the correct answer.

29.
$$\lim_{x \to \pi/2} \frac{\tan\left(\frac{\pi}{4} - \frac{x}{2}\right)(1 - \sin x)}{4\left(\frac{\pi}{4} - \frac{x}{2}\right)(\pi - 2x)^2}$$
$$= \frac{1}{32}.$$
Hence, (C) is the correct answer.

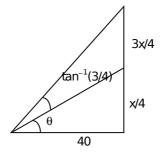
Therice, (C) is the correct answer.

32.
$$f(-x) = -f(x)$$

Hence, (B) is the correct answer.

1.
$$\sin (\theta + \alpha) = \frac{x}{40}$$

 $\sin a = \frac{x}{140}$
 $\Rightarrow x = 40$.
Hence, (B) is the correct answer



34.
$$f(x) = 0$$
 at $x = p$, q
 $6p^2 + 18ap + 12a^2 = 0$
 $6q^2 + 18aq + 12a^2 = 0$
 $f''(x) < 0$ at $x = p$
and $f''(x) > 0$ at $x = q$.

30. Applying L. Hospital's Rule
$$\lim_{x\to 2a} \frac{f(a)g'(a) - g(a)f'(a)}{g'(a) - f'(a)} = 4$$

$$\frac{k(g'(a) - ff'(a))}{(g'(a) - f'(a))} = 4$$

$$k = 4.$$

Hence, (A) is the correct answer.

36.
$$\int_{a}^{b} x f(x) dx$$

$$= \int_{a}^{b} (a+b-x) f(a+b-x) dx.$$
Hence, (B) is the correct answer.

- f'(0) 33. f'(0-h)=1f'(0 + h) = 0LHD ≠ RHD. Hence, (B) is the correct answer.
- $\lim_{x\to 0} \frac{\tan(x^2)}{x\sin x}$ 37. $= \lim_{x \to 0} \frac{\tan(x^2)}{x^2 \left(\frac{\sin x}{y}\right)}$ Hence (C) is the correct answer.

f' (0 + h) = 0
LHD
$$\neq$$
 RHD.
Hence, (B) is the correct answer.
37.
$$\lim_{x\to 0} \frac{\tan(x^2)}{x\sin x}$$

$$= \lim_{x\to 0} \frac{\tan(x^2)}{x^2\left(\frac{\sin x}{x}\right)}$$

$$= 1.$$
Hence (C) is the correct answer.
38.
$$\int_0^1 x (1-x)^n dx = \int_0^1 x^n (1-x)$$

$$= \int_0^1 (x^n - x^{n+1}) = \frac{1}{n+1} - \frac{1}{n+2}.$$
Hence, (C) is the correct answer.

35.
$$F(t) = \int_{0}^{t} f(t - y) f(y) dy$$

$$= \int_{0}^{t} f(y) f(t - y) dy$$

$$= \int_{0}^{t} e^{y} (t - y) dy$$

$$= x^{t} - (1 + t).$$
Hence, (B) is the correct answer.

34. Clearly f''(x) > 0 for $x = 2a \Rightarrow q = 2a < 0$ for $x = a \Rightarrow p = a$ or $p^2 = q \Rightarrow a = 2$. Hence, (C) is the correct answer.

40.
$$F'(x) = \frac{e^{\sin x}}{3^x}$$

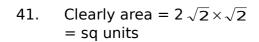
= $\int \frac{3}{x} e^{\sin x} dx = F(k) - F(1)$

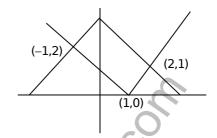
$$= \int_{1}^{64} \frac{e^{\sin x}}{x} dx = F(k) - F(1)$$

$$= \int_{1}^{64} F'(x) dx = F(k) - F(1)$$

$$F(64) - F(1) = F(k) - F(1)$$

$$\Rightarrow k = 64.$$
Hence, (D) is the correct answer.





45. Let p (x, y)
$$(x - a_1)^2 + (y - b_1)^2 = (x - a_2)^2 + (y - b_2)^2$$

$$(a_1 - a_2) x + (b_1 - b_2) y + \frac{1}{2} (b_2^2 - b_1^2 + a_2^2 - a_1^2) = 0.$$
 Hence, (A) is the correct answer.

46.
$$x = \frac{acost+bsint+1}{3}, y = \frac{asint-bcost+1}{3}$$

$$\left(x-\frac{1}{3}\right)^2 + y^2 = \frac{a^2+b^2}{9}.$$
 Hence, (B) is the correct answer.

43. Equation
$$y^2 = 4a \ 9x - h$$
)
$$2yy_1 = 4a \Rightarrow yy_1 = 2a$$

$$yy_2 = y_1^2 = 0.$$
Hence (B) is the correct answer.

42.
$$\int_{0}^{1} f(x) [x^{2} - f(x)] dx$$
solving this by putting $f'(x) = f(x)$.
Hence, (B) is the correct answer.

50. Intersection of diameter is the point
$$(1, -1)$$

$$\pi s^2 = 154$$

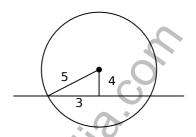
$$\Rightarrow s^2 = 49$$

$$(x - 1)^2 + (y + 1)^2 = 49$$
Hence, (C) is the correct answer.
47. (D)

49.
$$\frac{dx}{dy} (1 + y^2) = (e^{\sin^{-1} y} - x)$$
$$\frac{dx}{dy} + \frac{x}{1 + y^{\alpha}} = \frac{e^{\sin^{-1} - y}}{1 + y^2}$$

52.
$$\frac{x^2}{\left(\frac{12}{5}\right)^2} - \frac{y^2}{\left(\frac{9}{5}\right)^2} = 1$$
$$\Rightarrow e_1 = \frac{5}{4}$$
$$ae_2 = \sqrt{1 - \frac{b^2}{16}} \times 4 = 3$$
$$\Rightarrow b^2 = 7.$$

Hence, (C) is the correct answer.



69.
$$np = 4$$

$$npq = 2$$

$$q = \frac{1}{2}, p = \frac{1}{2}$$

$$n = 8$$

$$p(x = 1) = {}^{8}C_{1} \left(\frac{1}{2}\right)^{8}$$

$$= \frac{1}{32}.$$

Hence, (A) is the correct answer.

49.
$$(x-1)^2 + (y-3)^2 = r^2$$

 $(x-4)^2 + (y+2)^2 - 16 - 4 + 8 = 0$
 $(x-4)^2 + (y+2)^2 = 12$.

67. Select 2 out of 5 $= \frac{2}{5}.$ Hence, (D) is the correct answer.

65.
$$0 \le \frac{3x+1}{3} + \frac{1-x}{4} + \frac{1-2x}{2} \le 1$$

$$12x + 4 + 3 - 3x + 6 - 12x \le 1$$

$$0 \le 13 - 3x \le 12$$

$$3x \le 13$$

$$\Rightarrow x \ge \frac{1}{3}$$

$$x \le \frac{13}{3}$$

Hence, (C) is the correct answer.

3.
$$\operatorname{Arg}\left(\frac{z}{\omega}\right) = \frac{\pi}{2}$$
$$|z\omega| = 1$$
$$\overline{z}\omega = -i \text{ or } +i.$$